

*Proceedings of the 9th International Conference on Quality Software (QSIC 2009),  
IEEE Computer Society Press, Los Alamitos, CA (2009)*

## Automatic Generation of Normal Forms for Testing Object-Oriented Software\*

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**Abstract**—Testing object-oriented software is more complex than its procedural counterpart. The concept of “fundamental pairs” was introduced in our TACCLE methodology for testing object-oriented software. It was proved that, although the set of fundamental pairs is only a proper subset of equivalent ground terms, the use of fundamental pairs as test cases covers the use of equivalent ground terms. Recently, we found that any normal form consists of only a creator, or a creator followed only by constructors but not transformers; and yet the reverse is not necessarily true. Thus, the generation of patterns of normal forms is non-trivial and warrants further study. Motivated by this finding and based on further pattern analyses of normal forms and tree models with pruning techniques, we propose an algorithm to generate representative normal forms according to patterns and develop a corresponding automatic tool. This work improves the automation, coverage, and adequacy of selecting (equivalent) fundamental pairs as test cases.

**Keywords**—algebraic specification; object-oriented program; software testing; equivalent fundamental pair; normal form

### I. INTRODUCTION

The testing of object-oriented software requires new theories and techniques that are different from those for

its procedural counterpart [17]. Algebraic specifications have been used to generate test cases since the 1980s. The DAISTS system developed by Gannon et al. [9] inputs a tuple of arguments into both sides of an algebraic axiom, and employs a user-supplied equality function to check the output. An error is revealed when the outputs from the two sides do not agree.

A general theory for software testing based on algebraic specifications, including regularity, uniformity, and oracle hypotheses, was proposed by Bernot et al. [1]. Based on the theory, they developed a tool to generate test cases by replacing all the variables in the axioms with ground terms [1][2][6].

Doong and Frankl proposed an algebraic specification language LOBAS, which is more suitable for object-oriented programming. Based on LOBAS, a tool named ASTOOT was developed to generate class-level test cases, including equivalent terms through rewriting and non-equivalent terms by exchanging path conditions [7][8].

Following up on ASTOOT, Chen et al. [3][4][5] further proposed a methodology called TACCLE for object-oriented class-level testing. The concept of a *fundamental pair*, defined as a pair of terms constructed by replacing all the variables on both sides of an axiom by normal forms, is proposed. Obviously, the set of fundamental pairs is a proper subset of the set of equivalent ground terms. It is proved that a complete implementation of a canonical specification is consistent with respect to all equivalent terms if and only if it is consistent with respect to all fundamental pairs. In other words, the use of fundamental pairs as test cases covers the use of equivalent ground terms for the same purpose, and hence testers need only concentrate on the testing of fundamental pairs. In order to do this, an algorithm GFT has been proposed for generating finite number of equivalent fundamental pairs as test cases using axioms and normal forms. The normal forms used in the original GFT algorithm are generated manually.

The TACCLE project has attracted a lot of attention among researchers on software testing. More notable examples are [13][15][16][18][20][21].

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† This research is supported by a Union Grant of the Guangdong Province and National Natural Science Foundation of China (#U0775001), a Grant of National Natural Science Foundation of China (#60773083), grants of the Guangdong Province Science Foundation (#7010116 and #8151063201000022), and the General Research Fund of the Research Grant Council of Hong Kong (project no. 717308).

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Recently, we found that any normal form consists of only a creator, or a creator following only by constructors but not transformers; *but the reverse is not necessarily true*. Thus, the generation of representative normal forms is not trivial.<sup>1</sup> An algorithm and the corresponding tool to aid the generation of representative normal forms are necessary and significant. If the generated normal forms do not cover all possible patterns within a given length, the resulting tests will not be adequate. Based on pattern analysis, a tree model, and pruning technique, we propose an algorithm GNF to generate normal forms. We also implement a tool to aid the process.

This paper is organized as follows: Section 2 presents the basic concepts used in the paper. Section 3 describes the structural pattern analysis of normal forms. Section 4 investigates the generation of representative normal forms using Algorithm GNF and a computer-aided tool. Finally, Section 5 gives a conclusion.

## II. BASIC CONCEPTS

We summarize the basic concepts of algebraic specifications in this section. More details can be found in [3][4][5][10][11][14][19].

The syntax declaration and semantic definition are the two main components of an *algebraic specification* of a class. The *syntax declaration* specifies the input and output parameters of each operator. The *semantic definition* specifies the equational *axioms*, which describe the behavior related to each operator.

**Example 1.** The following example (from [3]) shows an algebraic specification of the class *IntStack* of integer stacks:

```

module INTSTACK
class IntStack
import classes
  Int
  Bool
operations
  new:  $\rightarrow$  IntStack
  _empty: IntStack  $\rightarrow$  Bool
  _push(): IntStack Int  $\rightarrow$  IntStack
  _pop: IntStack  $\rightarrow$  IntStack
  _top: IntStack  $\rightarrow$  Int  $\cup$  {NIL}
variables
  S: IntStack
  N: Int
axioms
  a1: new.empty = true
  a2: S.push(N).empty = false
  a3: new.pop = new
  a4: S.push(N).pop = S
  a5: new.top = NIL
  a6: S.push(N).top = N

```

A syntactically valid sequence of operations in a given algebraic specification is called a *term*. For example, *new.push(1).push(2).pop* is a term in the class of integer stacks above, but *new.push(1).push(2).top.pop* is not.

A term without variables is known as a *ground term*. In this paper, we will only consider ground terms because actual test cases do not involve variables.

Suppose a ground term  $u_0$  contains a sub-term  $v_0$  that is an instance of the left-hand side  $v$  of the axiom  $a: v = v'$ . Suppose further that, after replacing the sub-term  $v_0$  by the corresponding instance of the right-hand side  $v'$ , we obtain a new ground term  $u_1$ . Then, we say that the ground term  $u_0$  can be *transformed* into (or *rewritten* as) the ground term  $u_1$  using the axiom  $a$  as a *rewriting rule*. We denote this process by the notation  $u_0 \xRightarrow{(a)} u_1$ . For example,

$$\text{new.push(1).push(2).pop} \xRightarrow{(a_4)} \text{new.push(1)}.$$

A term is said to be a *normal form* if it cannot be transformed using any axiom in the specification. For instance, *new.push(1).push(2)* is a normal form but *new.push(1).push(2).pop* is not.

A *fundamental pair* is defined as a pair of terms generated by substituting all the variables on both sides of an axiom by their normal forms.

An algebraic specification is said to be *canonical* if any ground term will be transformed by the axioms in the specification into a unique normal form. For instance, the specification in Example 1 is canonical, but it is not if we change the axiom  $a_4$  to  $S = S.push(N).pop$ . We only discuss canonical specifications in this paper.

Two ground terms  $u_1$  and  $u_2$  in a canonical specification are said to be *equivalent* (denoted by  $u_1 \sim u_2$ ) if they have same normal form. For instance,

$$\text{new.push(1).push(2).pop} \sim \text{new.push(2).pop.push(1)}.$$

In a given class  $C$ , operations or methods generating new objects of  $C$  are called *creators*. Operations or methods changing the values of attributes of object in  $C$  are called *constructors* or *transformers*. The difference between constructors and transformers is that *constructors* can appear in normal forms but *transformers* cannot. Operations that only output the values of attributes of objects in  $C$  are called *observers*. In Example 1, for instance, the operation *new* is a creator, *\_push(N)* is a constructor, *\_pop* is a transformer, and *\_empty* and *\_top* are observers.

## III. PATTERN ANALYSIS OF NORMAL FORMS

### A. Properties of Normal Forms

The following important properties of normal forms follow directly from the definitions of terms, axioms, normal forms, constructors, and transformers:

<sup>1</sup> See, for instance, Example 2 and Proposition 4 in Section 3.2.

**Proposition 1.** For any sub-term  $t'$  of a term  $t$ , if  $t'$  is not a normal form, then  $t$  is not a normal form either.

**Proposition 2.** A term is not a normal form if any of its sub-terms matches the left-hand side of an axiom.

**Proposition 3.** A term is a normal form if none of its sub-terms matches the left-hand side of any axiom.

## B. A Case Study

We begin the investigation of structural patterns of normal forms with a case study.

**Example 2.** The following is an algebraic specification for a class *Book* in a simplified library system, where a book can only be reserved by one borrower. For ease of presentation, the side effects of some operations are omitted and some attributes are also omitted.

```

module BOOK
class Book
import classes
  String
  Integer
  Loc = {onShelf, atCounter, onLoan,
         onLoan&reserved}
operations
  newBook(, ): String Integer → Book
  // First parameter captures the name of the book;
  // second parameter captures the call number
  _name: Book → String
  _number: Book → Integer
  _location: Book → Loc
  _borrow: Book → Book
  _return: Book → Book
variables
  B: Book
  S: String
  I: Integer
axioms
  a11: newBook(S, I).name = S
  a12: newBook(S, I).number = I
  a13: newBook(S, I).location = onShelf
  a21: B.borrow.name = B.name
  a22: B.borrow.number = B.number
  a23: B.borrow = B if B.location
         = onLoan&reserved
  a24: B.borrow.location = onLoan
         if B.location ∈ {onShelf, atCounter}
  a25: B.borrow
         = newBook(B.name, B.number).borrow
         if B.location ∈ {onShelf, atCounter}
         and B ≠ newBook(, )
  a26: B.borrow.location = onLoan&reserved
         if B.location = onLoan
  a31: B.return.name = B.name
  a32: B.return.number = B.number

```

```

a33: B.return = B
         if B.location ∈ {onShelf, atCounter}
a34: B.return.location = onShelf
         if B.location = onLoan
a35: B.return.location = atCounter
         if B.location = onLoan&reserved
a41: B.borrow.return = B
         if B.location = onShelf

```

The normal form patterns of the class *Book* are analyzed as follows. For simplicity, we will use  $nw$ ,  $b$ , and  $r$  to denote  $newBook(S, I)$ ,  $borrow$ , and  $return$ , respectively. We will also use  $b^k$  to denote  $k$  consecutive  $borrow$  operations,  $r^j$  to denote  $j$  consecutive  $return$  operations, and “...” to denote a finite sequence of operations.

## Analysis.

- (1)  $nw$  is a normal form pattern because it cannot be rewritten according to any axiom.<sup>2</sup>
- (2)  $nw.b$  is also a normal form pattern because it cannot be rewritten according to any axiom.
- (3)  $nw.b^2$  is also a normal form pattern because it cannot be rewritten according to any axiom.
- (4) According to axioms  $a_{13}$ ,  $a_{24}$ , and  $a_{26}$ ,  $nw.b^2.location$  can be transformed into  $onLoan&reserved$ . As a result, according to axiom  $a_{23}$ , the term  $nw.b^3$  can be transformed into  $nw.b^2$ . Thus  $nw.b^3$  is not a normal form pattern.
- (5) Hence,  $nw.b^3...$  is not a normal form pattern.
- (6)  $nw.r$  is not a normal form pattern because  $nw.r \xRightarrow{(a_{13}, a_{33})} nw$ .
- (7) Hence,  $nw.r...$  is not a normal form pattern.
- (8)  $nw.b.r$  is not a normal form pattern because  $nw.b.r \xRightarrow{(a_{13}, a_{41})} nw$ .
- (9) Hence,  $nw.b.r...$  is not a normal form pattern.
- (10)  $nw.b^2.r$  is a normal form pattern because it cannot be rewritten according to any axiom.
- (11)  $nw.b^2.r.b$  is not a normal form pattern because  $nw.b^2.r.b \xRightarrow{(a_{13}, a_{24}, a_{26}, a_{35}, a_{25})} nw.b$ .
- (12) Hence,  $nw.b^2.r.b...$  is not a normal form pattern.
- (13)  $nw.b^2.r^2$  is not a normal form pattern because  $nw.b^2.r^2 \xRightarrow{(a_{13}, a_{24}, a_{26}, a_{35}, a_{33})} nw.b^2.r$ .
- (14) Hence,  $nw.b^2.r^2...$  is not a normal form pattern.

## Notes.

- (a) Each of the four normal form patterns ( $nw$ ,  $nw.b$ ,  $nw.b^2$ ,  $nw.b^2.r$ ) represents a set of normal forms of the class *Book*. For example,

$$nw.b^2.r = \{newBook(S, I).borrow.borrow.return \mid S \in String, I \in Integer\}.$$

<sup>2</sup> The term or any part of it does not match the left-hand side of any axiom.

- (b) Both *borrow* and *return* are constructors. There is no transformer in the class *Book*.
- (c) The above analysis covers all possible terms that consist of only a creator, or a creator followed only by constructors but not transformers.
- (d) The left-hand sides of the axioms  $a_{11}$ ,  $a_{12}$ ,  $a_{13}$ ,  $a_{21}$ ,  $a_{22}$ ,  $a_{24}$ ,  $a_{26}$ ,  $a_{31}$ ,  $a_{32}$ ,  $a_{34}$ , and  $a_{35}$  end with observers. They are transformed into normal forms representing the values of the attributes of the class *Book*.
- (e) The values of the *location* attribute of the normal forms patterns  $nw$ ,  $nw.b$ ,  $nw.b^2$ , and  $nw.b^2.r$  are *onShelf*, *onLoan*, *onLoan&reserved*, and *atCounter*, respectively.

From the above analysis and notes, we observe that the class *Book* has four and only four normal form patterns:

$newBook(S, I)$ ,  $newBook(S, I).borrow$ ,  
 $newBook(S, I).borrow.borrow$ , and  
 $newBook(S, I).borrow.borrow.return$ .

In Example 2, even though  $b$  and  $r$  are constructors of the class *Book*,  $nw.b^3$ ,  $nw.b.r$ ,  $nw.b^2.r^2$ ,  $nw.b^k.r^j...b^{k'}.r^{j'}.b^{k''}$  ( $k, \dots, k', k'', i, \dots, i' \geq 1$ ), and  $nw.b^k.r^j...b^{k'}.r^{j'}.b^{k''}.r^{j''}$  ( $k, \dots, k', k'', i, \dots, i', i'' \geq 1$ ) are not normal forms. Hence, we have:

**Proposition 4.** If a ground term  $T$  is a normal form of a class  $C$ , then  $T$  consists of either a creator of  $C$ , or a creator of  $C$  following only by constructors but not transformers of  $C$ . However, the converse does not hold.<sup>3</sup>

### C. More Examples

**Example 3.** The *normal form patterns* of the class *IntStack* in Example 1 are as follows:

$t_0: new$ ,  
 $t_1: new.push(N_1)$ ,  
 $t_2: new.push(N_1).push(N_2)$ ,  
 $t_3: new.push(N_1).push(N_2).push(N_3)$ ,  
 $t_4: new.push(N_1).push(N_2).push(N_3).push(N_4), \dots$

**Example 4.** The following, adapted from [4], is a simplified algebraic specification of a class *SavAcct1* of savings accounts in a banking system. For ease of presentation, some attributes are omitted and the side effects of some operations are ignored.

```
class SavAcct1
import classes
    Money
    String
operations
    newAc(, , ): String String Money → SavAcct1
```

```
// The input parameters denote the customer
// name, address, and account balance,
// respectively
name: SavAcct1 → String
address: SavAcct1 → String
balance: SavAcct1 → Money
setAddress(): SavAcct1 String → SavAcct1
credit(): SavAcct1 Money → SavAcct1
debit(): SavAcct1 Money → SavAcct1
```

#### variables

```
S, S': String
A: SavAcct1
M: Money
```

#### axioms

```
a1: newAc(S, S', M).name = S
a2: newAc(S, S', M).address = S'
a3: newAc(S, S', M).balance = M
a4: A.credit(M).balance = A.balance + M
a5: A.debit(M).balance = A.balance - M
    if A.balance ≥ M
a6: A.debit(M).balance = A.balance
    if A.balance < M
a7: A.setAddress(S).balance = A.balance
a8: A.credit(M).address = A.address
a9: A.debit(M).address = A.address
a10: A.setAddress(S).address = S
a11: A.credit(M).name = A.name
a12: A.debit(M).name = A.name
a13: A.setAddress(S).name = A.name
```

For simplicity, we will use  $new$ ,  $c$ ,  $d$ , and  $st$  to denote  $newAc$ ,  $credit$ ,  $debit$ , and  $setAddress$ , respectively. The *normal form patterns* are:

$new(S, S', M)$ ,  $new(S, S', M).c(M')$ ,  
 $new(S, S', M).d(M')$ ,  $new(S, S', M).st(S')$ ,  
 $new(S, S', M).op_1.op_2...op_k, \dots$

where each  $op_i$  is the pattern  $c(M_i)$ ,  $d(M_i)$ , or  $st(S_i)$ .

The notion of normal forms depends greatly on the system of axioms in the algebraic specification of a given class. When the axioms are changed, the set of normal forms may also be different. Consider, for instance, the simplified algebraic specification of the class *SavAcct1* of savings accounts in Example 4. Suppose we revise the axioms to produce a new specification *SavAcct2* as shown in Example 5 below. The set of normal forms will be significantly changed.

**Example 5.** The following is a simplified algebraic specification of another class *SavAcct2* of savings accounts in a banking system. Again, some attributes and side effects are omitted.

```
class SavAcct2
import classes
    Money
    String
```

<sup>3</sup> This does not contradict the statement “*constructors* can appear in normal forms but *transformers* cannot” in Section 2.

## operations

$newAc(\_, \_, \_): String\ String\ Money \rightarrow SavAcct2$   
 // The input parameters denote the customer  
 name, address, and account balance,  
 respectively  
 $name: SavAcct2 \rightarrow String$   
 $address: SavAcct2 \rightarrow String$   
 $balance: SavAcct2 \rightarrow Money$   
 $setAddress(\_): SavAcct2\ String \rightarrow SavAcct2$   
 $credit(\_): SavAcct2\ Money \rightarrow SavAcct2$   
 $debit(\_): SavAcct2\ Money \rightarrow SavAcct2$

## variables

$S, S': String$   
 $A: SavAcct2$   
 $M, M': Money$

## axioms

$a_1: newAc(S, S', M).name = S$   
 $a_2: newAc(S, S', M).address = S'$   
 $a_3: newAc(S, S', M).balance = M$   
 $a_4: A.credit(M).balance = A.balance + M$   
 $a_5: A.debit(M).balance = A.balance - M$   
 if  $A.balance \geq M$   
 $a_6: A.setAddress(S).balance = A.balance$   
 $a_7: A.credit(M).address = A.address$   
 $a_8: A.debit(M).address = A.address$   
 if  $A.balance \geq M$   
 // The condition makes  $a_8$  independent of  $a_{16}$   
 $a_9: A.setAddress(S).address = S$   
 $a_{10}: A.credit(M).name = A.name$   
 $a_{11}: A.debit(M).name = A.name$   
 if  $A.balance \geq M$   
 // The condition makes  $a_{11}$  independent of  $a_{16}$   
 $a_{12}: A.setAddress(S).name = A.name$   
 $a_{13}: A.credit(M).debit(M') = A.credit(M - M')$   
 if  $M > M'$   
 $a_{14}: A.credit(M).debit(M') = A.debit(M' - M)$   
 if  $M < M' \wedge A.balance \geq M' - M$   
 $a_{15}: A.credit(M).debit(M') = A$  if  $M = M'$   
 $a_{16}: A.debit(M) = A$  if  $A.balance < M$   
 $a_{17}: A.debit(M).credit(M') = A.credit(M' - M)$   
 if  $M \leq A.balance \wedge M < M'$   
 $a_{18}: A.debit(M).credit(M') = A.debit(M - M')$   
 if  $M \leq A.balance \wedge M > M'$   
 $a_{19}: A.debit(M).credit(M') = A$   
 if  $M \leq A.balance \wedge M = M'$   
 $a_{20}: A.credit(M).credit(M') = A.credit(M + M')$   
 $a_{21}: A.debit(M).debit(M') = A.debit(M + M')$   
 if  $M + M' \leq A.balance$   
 $a_{22}: A.setAddress(S_1).setAddress(S)$   
 $= A.setAddress(S)$

We will again use  $new$ ,  $c$ ,  $d$ , and  $st$  to denote  $newAc$ ,  $credit$ ,  $debit$ , and  $setAddress$ , respectively. The *normal form patterns* are:

$new(S, S', M)$ ,  
 $new(S, S', M).c(M')$ ,  
 $new(S, S', M).d(M')$ ,  
 $new(S, S', M).st(S')$ ,  
 $new(S, S', M).st(S_1).op_1.st(S_2).op_2...st(S_k).op_k$ ,

$new(S, S', M).st(S_1).op_1.st(S_2).op_2...st(S_k)$ ,  
 $new(S, S', M).op_1.st(S_1).op_2.st(S_2)...op_k.st(S_k)$ ,  
 $new(S, S', M).op_1.st(S_1).op_2.st(S_2)...op_k$ , ...

where  $op_i$  is one of the patterns  $c(M_i)$  or  $d(M_i)$ . Notice that, although  $c$  and  $d$  are constructors, ground terms of the form  $new.op_1.op_2...op_k$  (where  $k > 1$  and each  $op_i$  is one of the patterns  $c(M_i)$  or  $d(M_i)$ ) are not normal forms as they can be rewritten as one of the patterns  $new.c(M)$  or  $new.d(M)$ .

## IV. GENERATING NORMAL FORMS FROM PATTERNS

From Proposition 4 and the examples above, we realize that the generation of normal form patterns is non-trivial. This section presents an algorithm GNF and a corresponding tool to aid the generation process. The algorithm requires the following additional definitions.

### A. Principal Operators, Normal Forms, and Axioms

It is obvious from the definitions of creators, constructors, transformers, and observers that, by using only the syntax declaration in the algebraic specification of a given class, we can distinguish creators and observers from each other, and also distinguish them from constructors and transformers. We cannot, however, distinguish constructors and transformers from each other using only the syntax declaration. We need to use the semantic definitions in the algebraic specification for this purpose. For this reason, we propose to bundle constructors and transformers together, thus:

**Definition 1 (Principal Operator).** We refer to a constructor or transformer in the algebraic specification of a class  $C$  as a *principal operator* of  $C$ .

In Example 1, the normal form of the term  $new.push(1).push(2).top$  is 2. It is, in fact, a value of the attribute  $top$  of the class  $IntStack$ . We do not consider such kind of simple normal form in this paper. We only consider *principal normal forms*, which are defined as follows:

**Definition 2 (Principal Normal Form).** A normal form in the algebraic specification of a class  $C$  is known as a *principal normal form* of  $C$  if it ends with a principal operator of  $C$ .

Obviously, a principal normal form of  $C$  returns an object of class  $C$ .

**Definition 3 (Principal Axiom).** An axiom in the algebraic specification of a class  $C$  is called a *principal axiom* if its left-hand side ends with a principal operator of  $C$ , and is called an *attributive axiom* if its left-hand side ends with an observer of  $C$ .

In example 1, for instance,  $a_4$  is a principal axiom and  $a_6$  is an attributive axiom.

**Definition 4 (Length).** The number of operators in a given normal form is known as the *length* of the normal form.

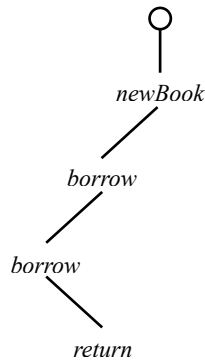
In Example 2, for instance, the length of the normal form  $newBook(S, I).borrow.borrow.return$  is 4.

### B. Tree model

In this subsection, we set up a tree model for principal normal forms.

**Definition 5 (Principal Normal Form Pattern Tree).** Suppose the algebraic specification of a given class  $C$  contains creators  $cr_1, cr_2, \dots, cr_i$ , and principal operators  $pr_1, pr_2, \dots, pr_j$ . We construct a tree  $T_C$  using the following procedure:

- (i) Construct a node “ $\circ$ ” as the root, and take  $cr_1, cr_2, \dots, cr_i$  as child nodes of “ $\circ$ ”.
- (ii) For each node  $cr_k$  ( $k = 1, 2, \dots, i$ ), take  $pr_1, pr_2, \dots, pr_j$  as its child nodes.
- (iii) For each node  $pr_m$  ( $m = 1, 2, \dots, j$ ), take  $pr_1, pr_2, \dots, pr_j$  again as its child nodes, and so on.
- (iv) The sequence of operators in the nodes along a path from the root “ $\circ$ ” to any node  $n_r$  is a term of  $C$ . We refer to this term as an *associated term* of the node  $n_r$ . For any given node  $n_s$ , if its associated term  $t_s$  is not a normal form, we can conclude from Proposition 1 that the associated terms for all child nodes of  $n_s$  are all not normal forms either. Hence, we remove  $n_s$  and any of its child nodes from the tree  $T_C$ . In other words, we *prune* the subtree with root  $n_s$ . The associated terms of the remaining nodes are normal forms.



**Figure 1.** Principal normal form pattern tree for the class *Book* in Example 2.

We refer to the tree  $T_C$  constructed by the above procedure with pruning as the *principal normal form pattern tree* of class  $C$ . In fact, it is a model of the structural pattern of the principal normal forms of  $C$ .

We note also the following:

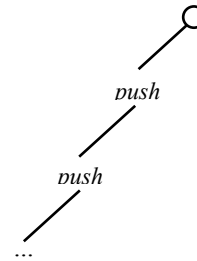
- (a) In step (4) of Definition 5, we can use Proposition 2 to determine that an associated term  $t$  of a node is not a normal form, and use Proposition 3 to determine that an associated term  $t$  is a normal form. Since we construct the tree  $T_C$  top-down, we need only check whether the *current* associated term  $t$  matches with the left-hand sides of axioms. We need not check this for the proper sub-terms of  $t$ , as all the proper sub-terms of  $t$  have already been verified to be normal forms.
- (b) Step (4) in Definition 5 provides a *pruning rule* for principal normal form pattern trees.
- (c) A principal normal form pattern tree may be finite or infinite. In the following figures, “...” denotes potentially infinite subtrees.

**Example 6.** A principal normal form pattern tree for the class *Book* in Example 2 is shown in Figure 1.

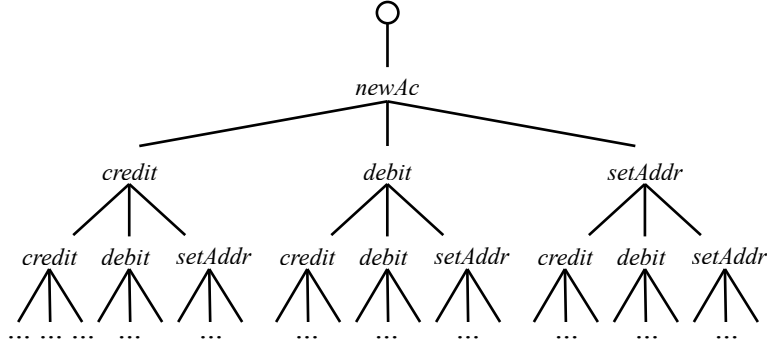
**Example 7.** A principal normal form pattern tree for the class *IntStack* in Example 3 is shown in Figure 2.

**Example 8.** A principal normal form pattern tree for the class *SavAcct1* in Example 4 is shown in Figure 3.

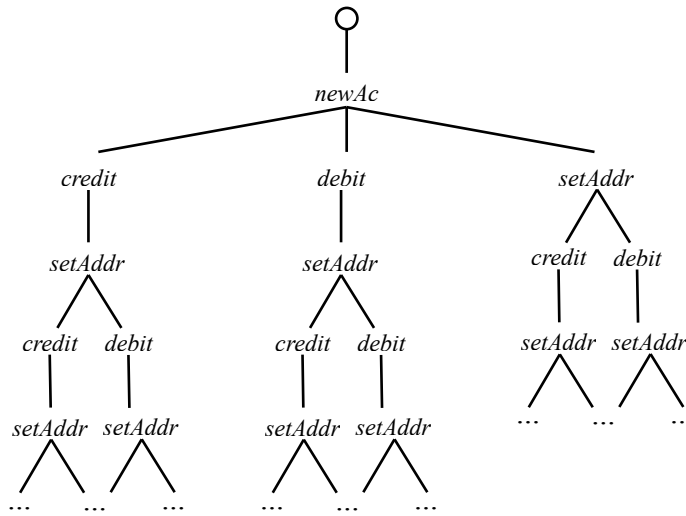
**Example 9.** A principal normal form pattern tree for the class *SavAcc2* in Example 5 is shown in Figure 4.



**Figure 2.** Principal normal form pattern tree for the class *IntStack* in Example 3.



**Figure 3.** Principal normal form pattern tree for the class *SavAcct1* in Example 4.



**Figure 4.** Principal normal form pattern tree for the class *SavAcct2* in Example 5.

### C. Algorithm GNF

We can now describe Algorithm *GNF* to aid the Generation of principal Normal Form patterns from the algebraic specification of a given class *C*. The fundamental concept behind the algorithm is as follows: In order to generate principal normal form patterns for class *C*, we need only enumerate the associated terms by traversing the nodes in the principal normal form pattern tree of class *C* using a top-down breadth-first strategy in conjunction with the pruning technique described in Section 4.3. On the other hand, we need not actually construct and store the tree structure. The tree model simply helps us visualize the (traversing) strategy and the (pruning) technique. We need not even refer to the notions of *trees*, *paths*, *nodes*, or *associated terms* in the actual algorithm.

#### Algorithm GNF.

(1) Analyze the syntax declaration of the algebraic specification of class *C* (or interact with the requirements

analyst) to determine the set *CR* of creators and the set *CT* of principal operators. (They may contain parameters.) Obtain the set *AX* of principal axioms of the algebraic specification.

- (2) Ask the requirements analyst or tester to specify the maximum length *Lmax* of the target principal normal forms, where  $Lmax \geq 1$ .
- (3) Let *PPNF* denote the set of all *Potential Principal Normal Form patterns* generated so far, *PPNF0* denote the set of the *Potential Principal Normal Form patterns* generated in the last execution of step (4), and *PPNF1* denote the set of the *Potential Principal Normal Form patterns* that will be generated in the next execution of step (4). Initialize *PPNF* to  $CR^4$ , *PPNF0* to *CR*, and *PPNF1* to  $\emptyset$ , where the parameters for each  $cr \in CR$  are bound to the corresponding variables. Let *L* denote the maximum length of the principal normal forms in

<sup>4</sup> Obviously, creators must be principal normal forms.

the current *PPNF*. Initialize  $L$  to 1.

- (4) For each  $t \in PPNF0$ , do {
    - For each  $ct \in CT$  (where the parameters in  $ct$  are all be bound to corresponding variables), do {
      - If  $t.ct$  can *match*<sup>5</sup> the left-hand side of an axiom in  $AX$ 
        - skip the term  $t.ct$ ;<sup>6</sup>
        - Else,  $PPNF1 = PPNF1 \cup \{t.ct\}$ ;<sup>7</sup>
  - If  $PPNF1 \neq \emptyset$ , {
    - $L = L + 1$ ;
    - $PPNF = PPNF \cup PPNF1$ ;
  - $PPNF0 = PPNF1$ ;
  - $PPNF1 = \emptyset$ ;
- (5) If  $L \neq Lmax$  and  $PPNF0 \neq \emptyset$ , go to (4);
  - (6) Interact with the requirements analyst or tester to review the *PPNF* and produce a set *FPNF* of *Final Principal Normal Form patterns* of the given class  $C$ .
  - (7) Output the *FPNF*.

We note that the concept of *term matching* in step (4) of Algorithm *GNF* is also known as *unification* in artificial intelligence. Effective algorithms for unification can be found in standard texts on logic programming. In fact, if Prolog were used to implement Algorithm *GNF*, the term matching process would be rather simple. The drawback, of course, would be the user interface.

In step (2) of Algorithm *GNF*, if the target maximum length  $Lmax$  of principal normal forms specified by the requirements analyst or tester is greater than the actual maximum length of principal normal forms of the given class<sup>8</sup>, the execution of Algorithm *GNF* will be automatically terminated by the condition  $PPNF0 = \emptyset$  in step (5). If the actual maximum length of principal normal forms of the given class is infinite, or is larger than the target maximum length  $Lmax$ , then Algorithm *GNF* will enumerate principal normal forms from a length of 1 to the given length  $Lmax$ .

For a given class, the numbers of creators, principal operators, and principal axioms are not large in general, and hence the number of loops in Algorithm *GNF* is not large. Furthermore, the pruning technique in *GNF* significantly improves the efficiency of the algorithm.

<sup>5</sup> We need not check whether each proper sub-term of  $t.ct$  can match with the left-hand side of an axiom in  $AX$ , as it has been checked in a previous execution of step (4).

<sup>6</sup> This is equivalent to pruning in the tree model. The term  $t.ct$  here is not a normal form.

<sup>7</sup> According to Proposition 3, the term  $t.ct$  here must be a principal normal form.

<sup>8</sup> In Example 2, for instance, the actual maximum length of the principal normal forms of the class *Book* is 4.

#### D. Computer-Aided Tool *GNF*

A prototype computer-aided tool *GNF* for the algorithm has been implemented using Java in *JDK-6-windows-i586* on *Eclipse-SDK-3.2.1-win32* under *Microsoft Windows XP*. It contains eight main class modules, namely *TxtFile*, *FileTransformer*, *XmlFile*, *Specification*, *StringTransformer*, *ConditionHandler*, *NormalformGenerator*, and *OutputNF*. The algebraic specifications are expressed in *XML*.

Experiments have been conducted on the classes *Book*, *IntStack*, *SavAcct1*, and *SavAcct2*, and have generated 4, 20, 40, and 30 principal normal forms, respectively. The experimental results are shown in Figures 1 to 4, respectively, and confirm the analyses in Examples 2 to 5, respectively. More details can be found in [11].

#### V. LIMITATION AND FUTURE WORK

In this paper, we assume that any given specification of a class must be canonical with proper imports. We have explained in our earlier paper [4] that this assumption is reasonable.

As future work, we will consider the optimization of Algorithm *GNF*, an implementation of this optimized algorithm in Prolog, and more experiments on the new implementation.

#### VI. CONCLUSION

The testing of equivalent fundamental pairs is an effective approach for object-oriented class level testing. However, in the previous algorithm for selecting equivalent fundamental pairs, normal forms have to be supplied manually. We find that the structural patterns of normal forms and their generation are nontrivial. Hence, a new algorithm is necessary for improving the coverage of normal forms and the efficiency of testing fundamental pairs.

Based on normal form patterns, a tree model, and a pruning technique, this paper presents an algorithm to generate representative normal forms. A corresponding computer-aided tool has been developed. Experimentation shows that it can cover patterns of normal forms within a user-defined maximum length. The pruning technique based on the tree model improves the time and space performances of the tool.

#### ACKNOWLEDGMENT

Our thanks are due to Miss Mei-Ling He for her contributions to the implementation and experimentation of the prototype tool *GNF*.

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